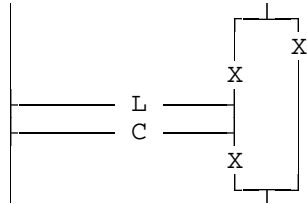


Appendix D Coupled Triplets

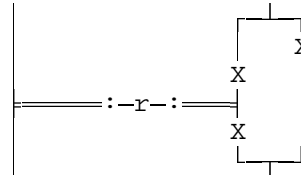
The circuit editor is equipped to convert many conventional transmission zero networks into coupled triplet networks which utilize coupling between alternate "resonators" to produce the zeros. The coupled triplet networks look like this:

With lumped component
resonator:



X may be either L or C.

With transmission line
resonator:



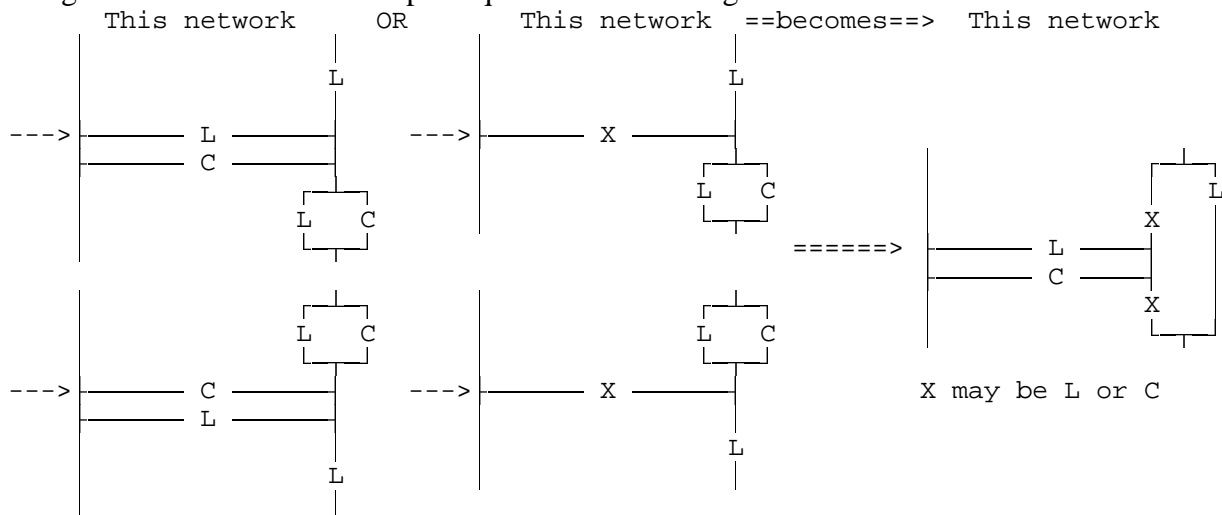
The editor command for the coupled triplet transformation is **[MIS1:] Triplet** followed by the branch number of the single shunt component, a shorted stub "resonator" or the lowest branch number of a shunt L-C "tank resonator" pair.

On networks having a parallel L and C, an impedance transformation can be specified to scale the network impedance from the "triplet" through to the termination. The prompt will look like this after the **Triplet** command is given:

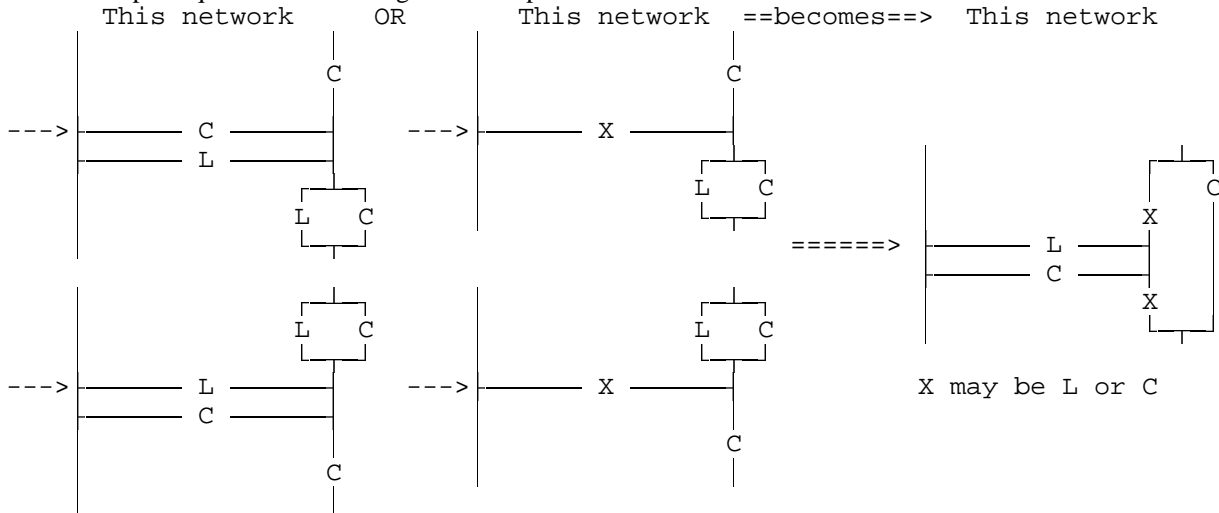
(Cr = 1.0) Impedance ratio at triplet?

The same editor command (Triplet) will allow the values in the shunt "resonator" of the triplet network itself (in "triplet" form) to be forced to any desired value. Some situations will result in negative values however.

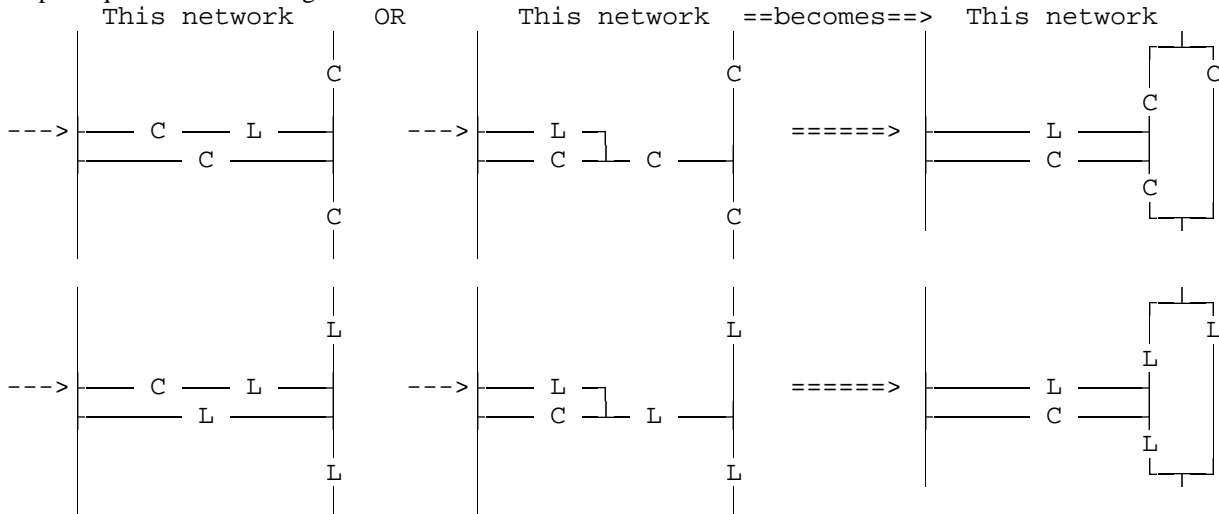
The possible conventional networks that are compatible with the coupled triplet are shown below. In all cases when performing these transformations you must specify the branch number marked by the arrow. Note that this transformation can not be reversed later. It can be undone by using the "oops" command however. Oops will undo the last 10 commands. If you are not comfortable with the transformations that are to follow and would like to be able to back up directly to a point before the Triplet command, you can also use the **Save** command to save the network before the Triplet command is given. You can recall it later using the **Recall** command. Triplet equivalents involving a series inductor:



Triplet equivalents involving a series capacitor:

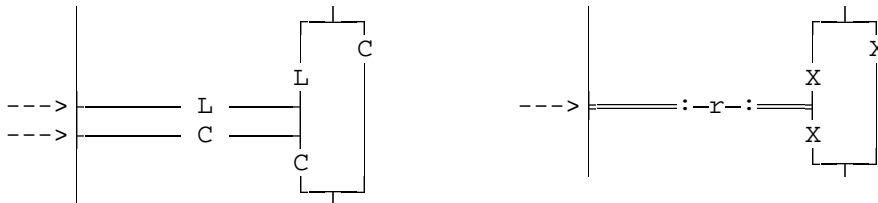


Triplet equivalents involving shunt notches:



Triplet shunt value transform

The two arrows in the L-C triplet network shown below identify the shunt L-C "tank" components. In several cases, one or the other of these two parts will be an open component that can simply be left out of the realization. That is, a huge inductor or a tiny capacitor. In other cases, it is possible to directly specify the value of either of these two parts. The **Triplet** command is also used for this function. Specify the branch number of the part whose value is to be forced. The program will prompt you for the value you want. The other will be adjusted to compensate. The impedance of a transmission line resonator may be forced as well.

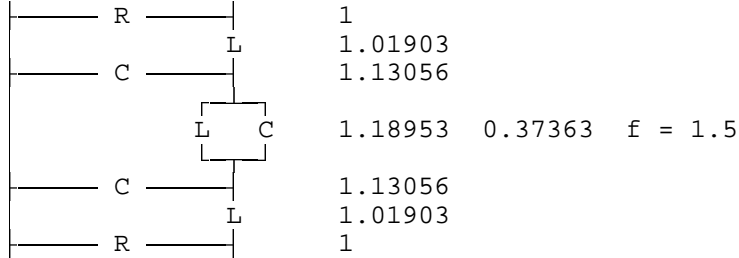


*** Example 1 ***

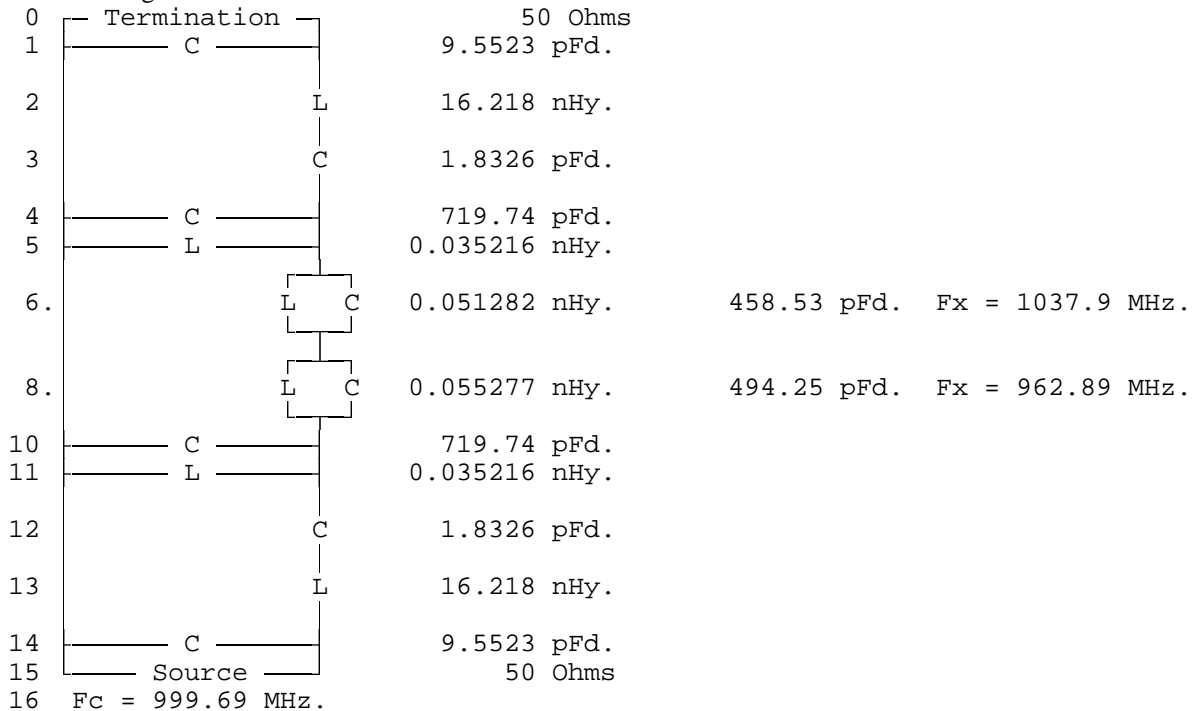
Design = Basic direct scaled bandpass (Using the reference lowpass placer)

```
passband Ripple (0=Butt. dB) 0.05
arithmetic Fo.           MHz. 1000
Bandwidth                MHz. 50
design Zo.                5
Source zo.               50
Termination zo.          50
config: Ser. Par. Tee Delta S
tType: 1=sing 2=doub 3=ratio 2
--- POLE PLACER DATA ---
Zeros at Infinity = 3
Finite transmission zero frequencies:
    1.500
Finite transmission zero sequence: 1
Placer specification mask:
```

Lowpass reference used:



The resulting bandpass is shown below. Note that the matcher was used to match the 5 Ohm design impedance to 50 Ohms before entering the circuit editor.



The first step is to raise the impedance at the series "trap" pair to get better capacitor values.

[NORT:] Xform branch 12

Preset ratio = 1.0000

What ratio ? 50

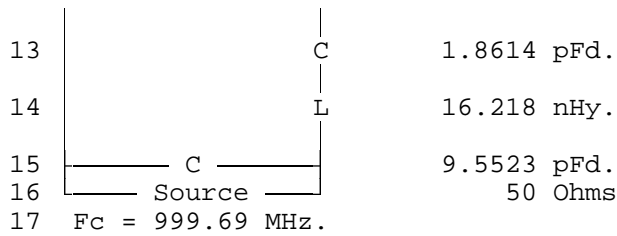
0	Termination	2500 Ohms		
1	C	0.19105 pFd.		
2	L	810.92 nHy.		
3	C	0.036653 pFd.		
4	C	14.395 pFd.		
5	L	1.7608 nHy.		
6.	L C	2.5641 nHy.	9.1706 pFd.	Fx = 1037.9 MHz.
8.	L C	2.7638 nHy.	9.8849 pFd.	Fx = 962.89 MHz.
10	C	14.172 pFd.		
11	L	1.7608 nHy.		
12	C	0.25918 pFd.		
13	C	1.5735 pFd.		
14	L	16.218 nHy.		
15	C	9.5523 pFd.		
16	Source	50 Ohms		
17	Fc = 999.69 MHz.			

Next, prepare the network for a triplet by getting rid of the capacitor at branch 10.

[NORT:] Interchange branches 10,11

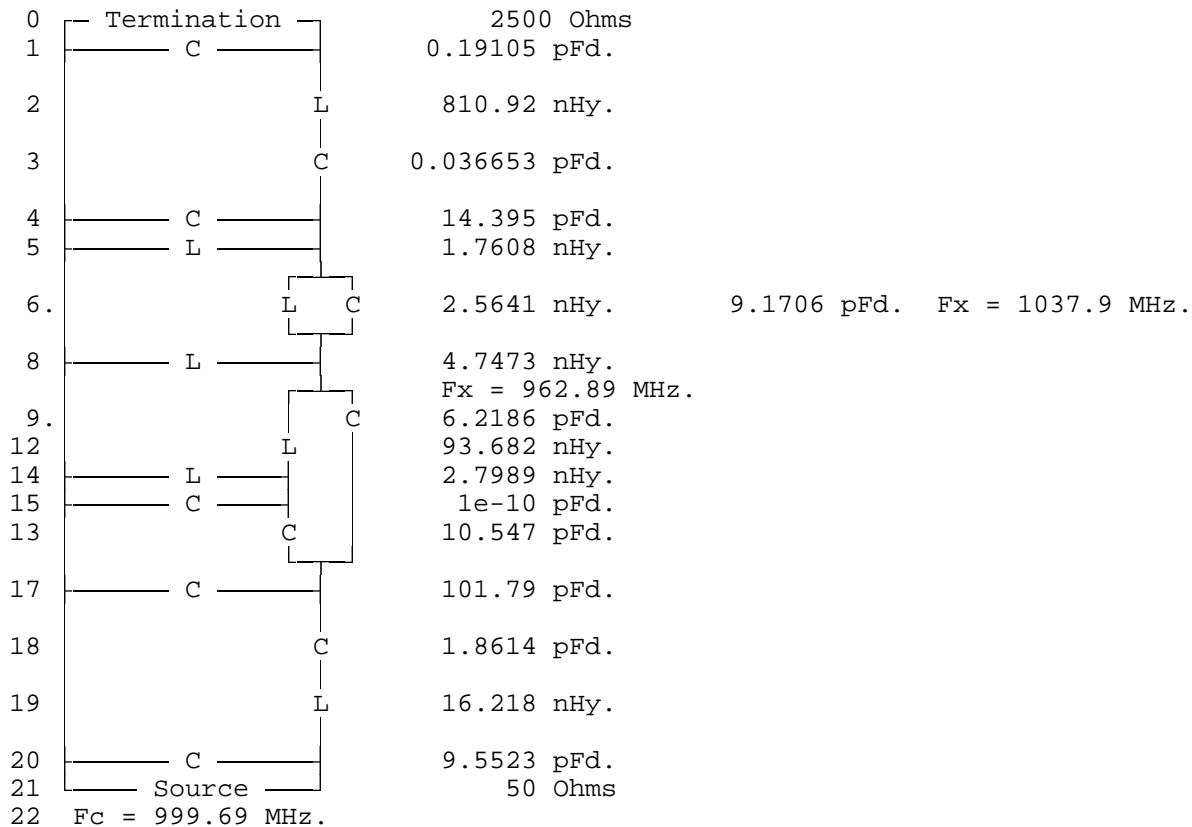
[NORT:] Pi-T at branch 12

0	Termination	2500 Ohms		
1	C	0.19105 pFd.		
2	L	810.92 nHy.		
3	C	0.036653 pFd.		
4	C	14.395 pFd.		
5	L	1.7608 nHy.		
6.	L C	2.5641 nHy.	9.1706 pFd.	Fx = 1037.9 MHz.
8.	L C	2.7638 nHy.	9.8849 pFd.	Fx = 962.89 MHz.
10	L	1.7608 nHy.		
11	C	16.766 pFd.		
12	C	101.79 pFd.		



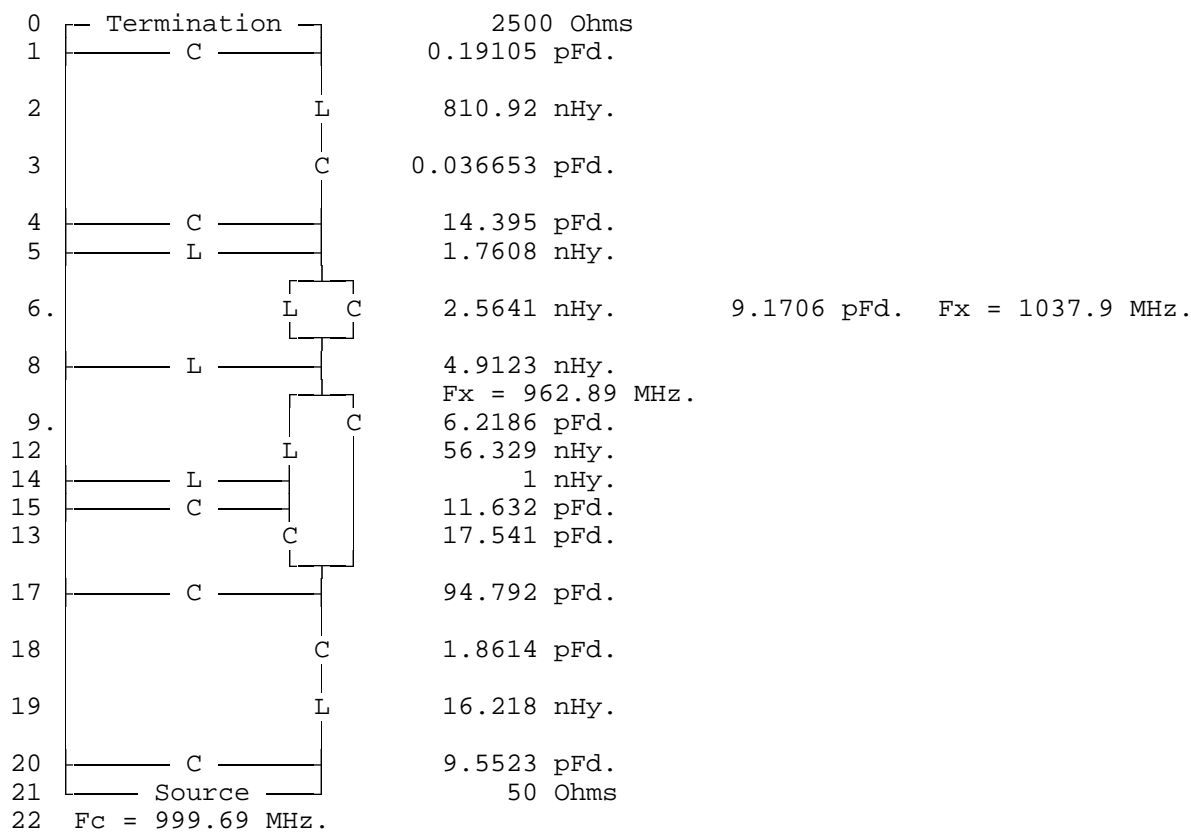
The network between branches 8 and 11 is now ready to be converted to a coupled triplet using the **Triplet** command.

[MIS1:] Triplet at branch 10

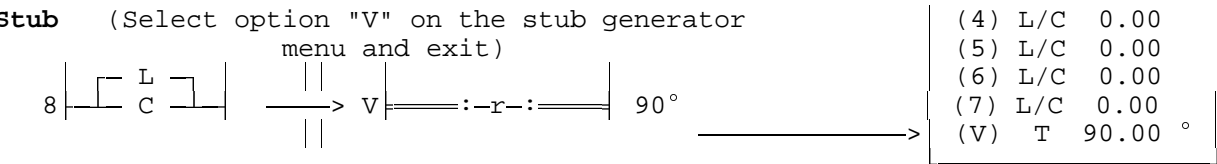


The L-C resonator at branches 14 and 15 must be modified by forcing some lower value inductor at branch 14. As the network is now, the capacitor at branch 15 is an open circuit, which the "LC to stub generator" that will be used next, can't handle. The value of 1 nHy was picked only because it is less than what is there now. This will ensure a reasonable capacitor value at branch 15.

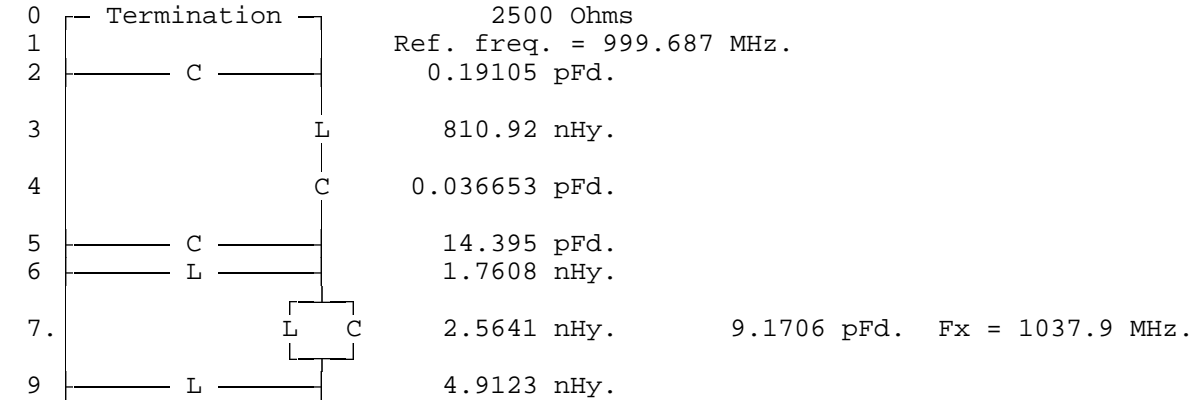
[MIS1:] Triplet at branch 14
 (Cr) to abort * What is new value (nHy.) ? 1

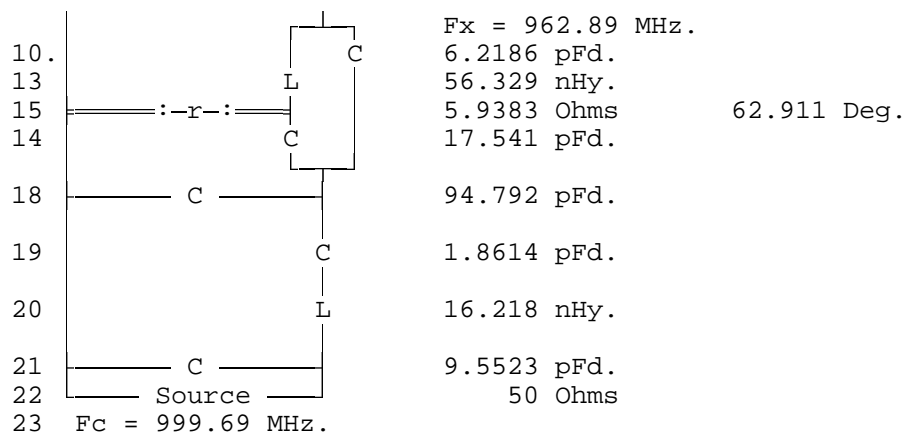


Next, the L-C resonator will be replaced by a shorted stub resonator. The "LC to stub generator" must first be programmed using the >PS command. Select option "V" on the stub generator menu. The actual replacement of the L-C network by a stub is done using the **Stub** command.



[MIS3:] Stub at branch 14

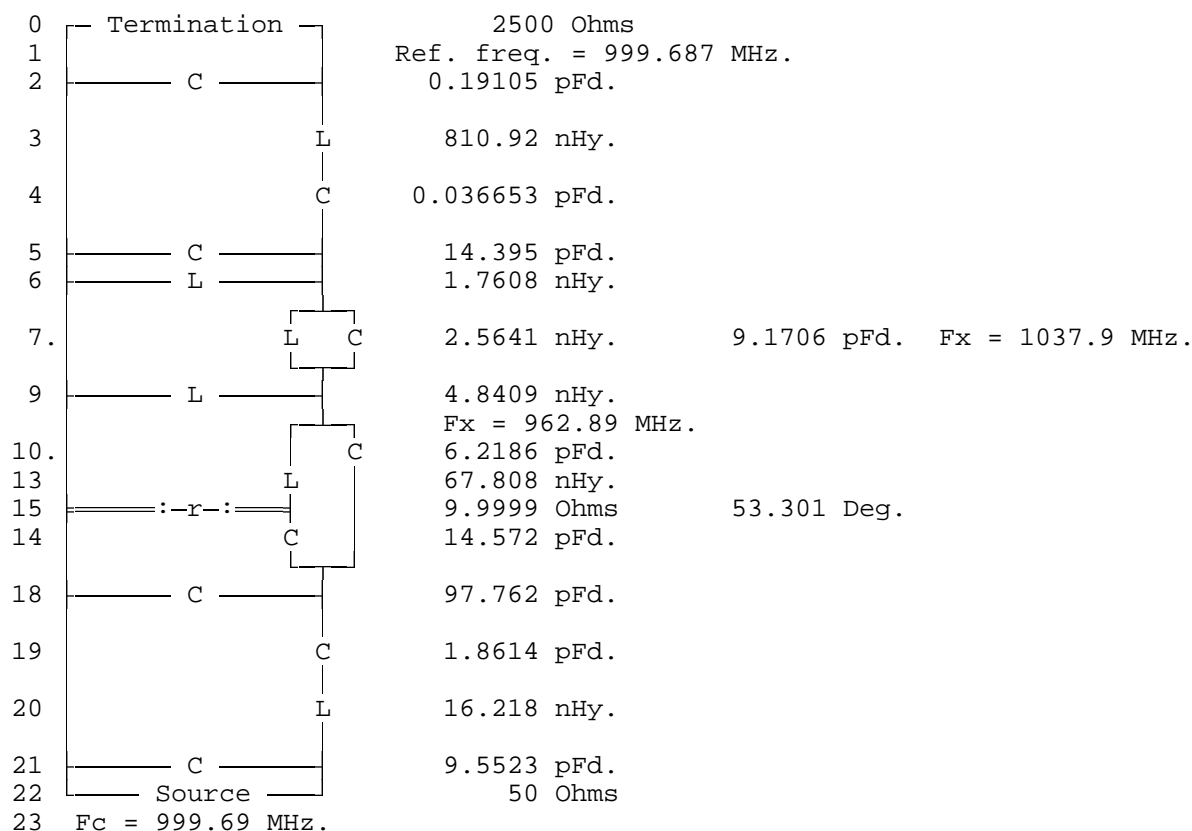




The final impedance of the stub resonator will be set later. For now we will use the **Triplet** command to preset it to 10 Ohms (which is roughly the impedance of a quarter wave ceramic resonator) to verify that the values are within acceptable range.

[MIS1:] Triplet at branch 15

(Cr) to abort * What is new value (Ohms) ? 10

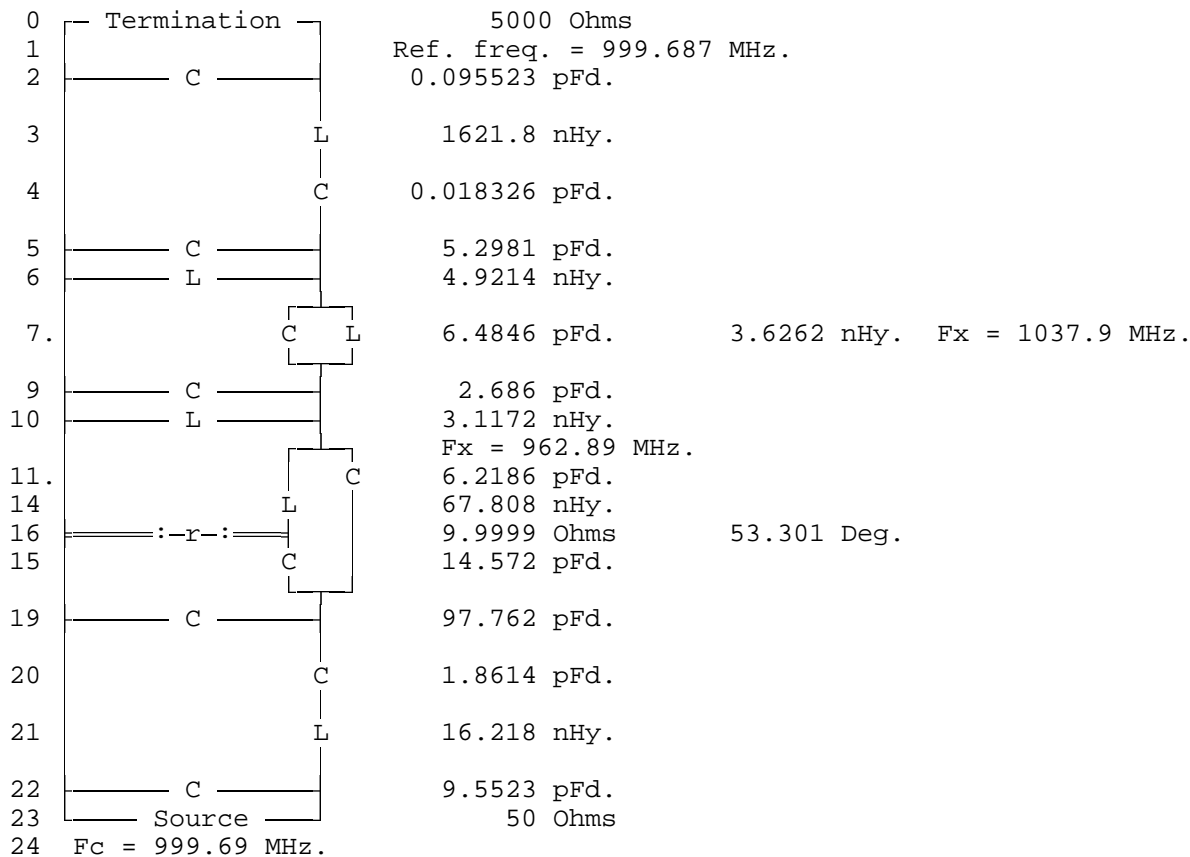


It is advisable to have a capacitor to ground next to the inductor at branch 9 to absorb its distributed capacity and to provide a binding post to connect the adjacent components. A Norton transform at the second series "trap" will generate this capacitor. The ratio can be

any value greater than 1.0 to ensure a positive value.

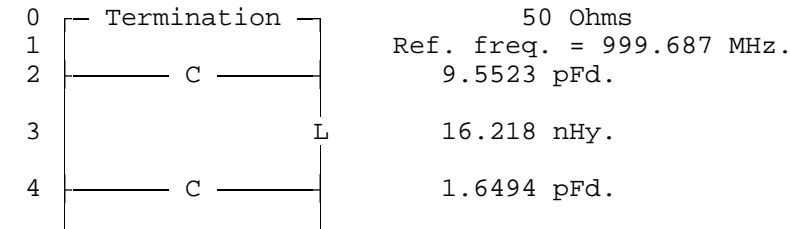
[NORT:] Xform at branch 7

Preset ratio = 1.0000
 What ratio ? 2

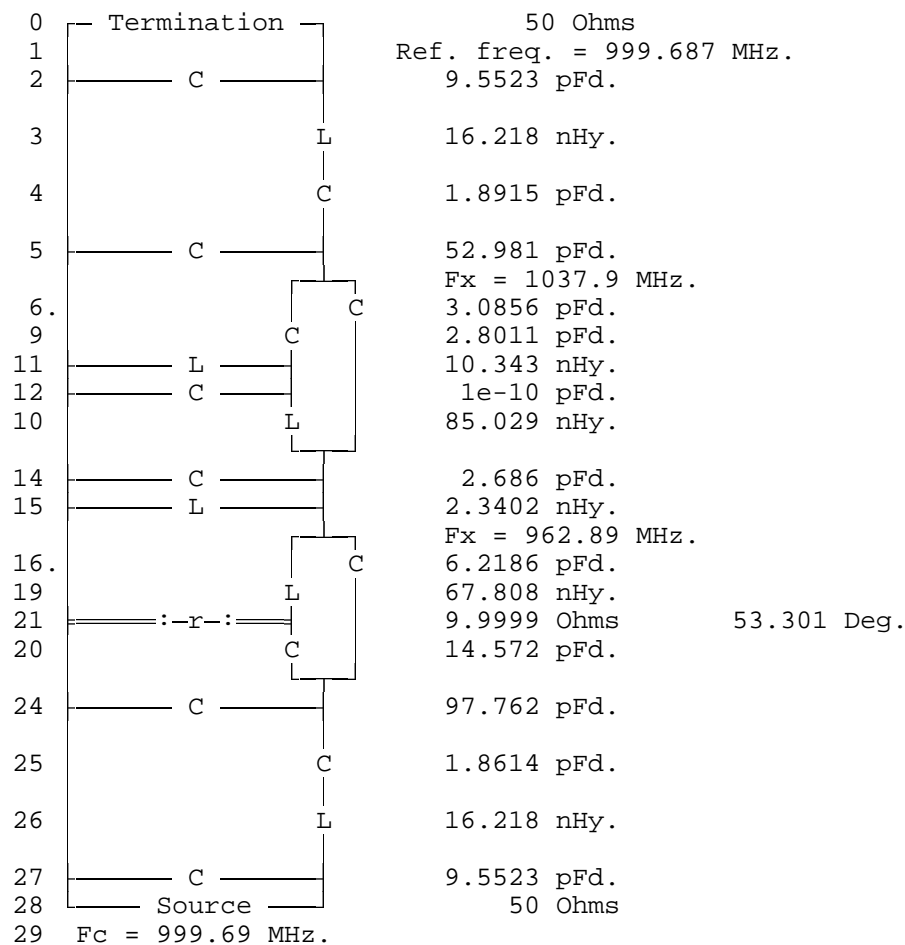


At this point, we will need to bring the termination impedance back to 50 ohms. To do this, the **Ratio** command will be used to set the "preset ratio" to that of the source to termination. Once this ratio is set, a Norton transform will restore the termination impedance. Note that <Enter> instructs the program to use the "Preset ratio" just established with the **Ratio** command or simply select the [OK] button.

[NORT:] Ratio of branches 23,0
 [NORT:] Xform at branch 4
 Preset ratio = .005
 What ratio ? <Enter> (Use preset ratio)



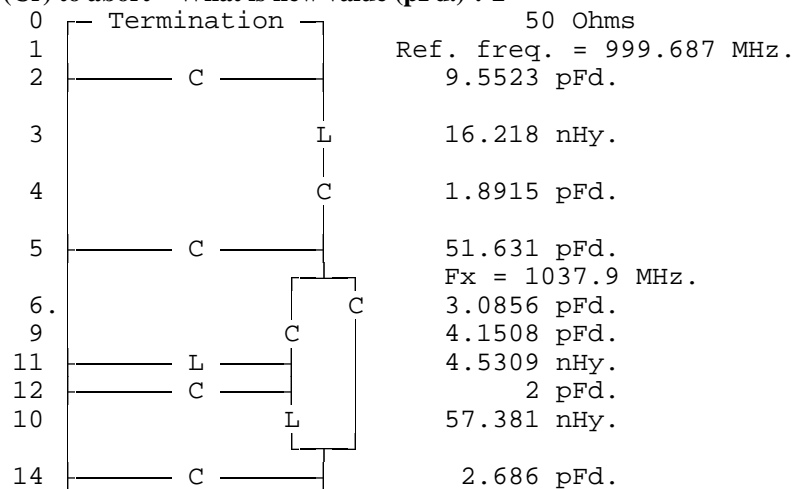
[MIS1:] Triplet at branch 7



As with the first triplet, the open capacitor at branch 12 must be brought up to something realistic. This time we will force it directly to 2 pFd.

[MIS1] Triplet at branch 12

(Cr) to abort * What is new value (pFd.) ? 2



15	L	2.3717 nHy.	
16.		Fx = 962.89 MHz.	
19	C	6.2186 pFd.	
21	L	67.808 nHy.	
20	C	9.9999 Ohms	53.301 Deg.
24	C	14.572 pFd.	
25	C	97.762 pFd.	
26	L	1.8614 pFd.	
27	L	16.218 nHy.	
28	C	9.5523 pFd.	
29	Source	50 Ohms	
	Fc = 999.69 MHz.		

The "LC to stub generator" will still be programmed from its first use. The L-C resonator can now be converted to a shorted stub using the **Stub** command.

[MIS3:] Stub at branch 11

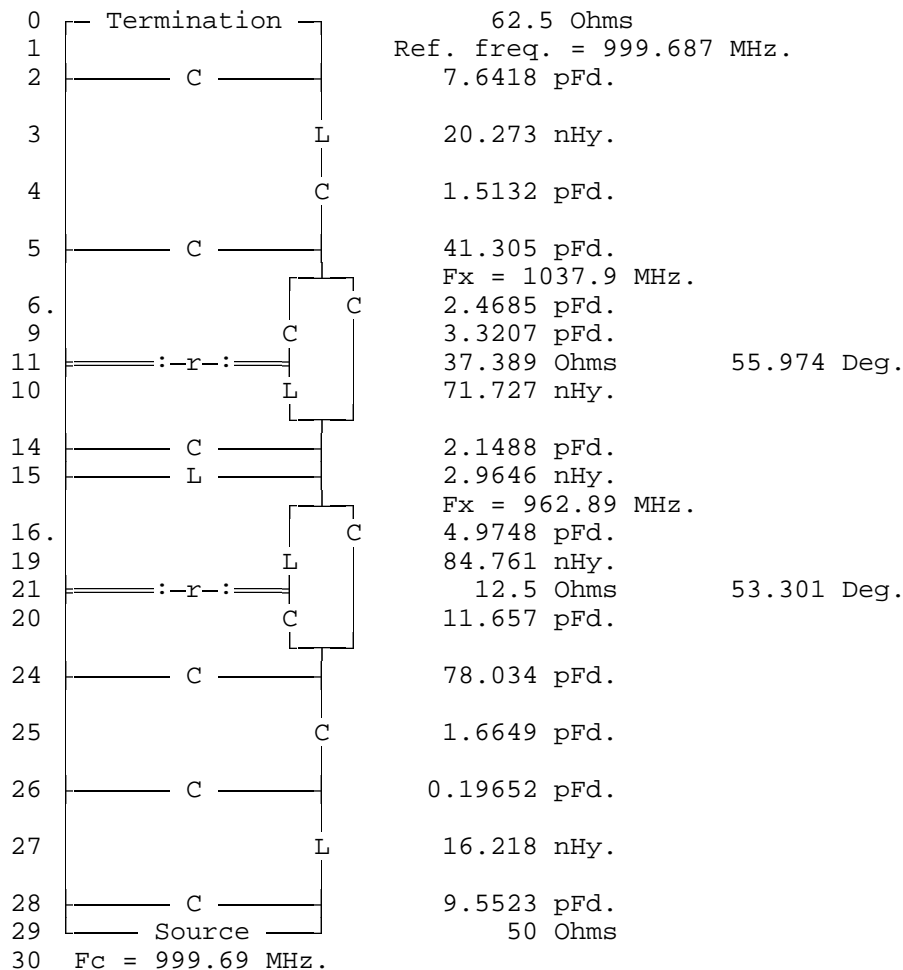
0	Termination	50 Ohms	
1		Ref. freq. = 999.687 MHz.	
2	C	9.5523 pFd.	
3	L	16.218 nHy.	
4	C	1.8915 pFd.	
5	C	51.631 pFd.	
6.	C	Fx = 1037.9 MHz.	
9	C	3.0856 pFd.	
11	L	4.1508 pFd.	
10	L	29.911 Ohms	55.974 Deg.
14	C	57.381 nHy.	
15	L	2.686 pFd.	
16.	C	2.3717 nHy.	
19	C	Fx = 962.89 MHz.	
21	L	6.2186 pFd.	
20	C	67.808 nHy.	
24	C	9.9999 Ohms	53.301 Deg.
25	C	14.572 pFd.	
26	L	97.762 pFd.	
27	L	1.8614 pFd.	
28	L	16.218 nHy.	
29	C	9.5523 pFd.	
	Source	50 Ohms	
	Fc = 999.69 MHz.		

The distributed capacity at the "hot nodes" between branches 3, 4 and branches 25, 26 to ground can be absorbed by shunt capacitors that can be added by transforming the entire triplet network up slightly in impedance and then back down with two Norton transforms, one on either side of the triplet pair. The ratio is picked just high enough to generate capacitors with good values. 1.25 and its reciprocal of .8 will be used.

[NORT:] Xform at branch 25

Preset ratio = .005

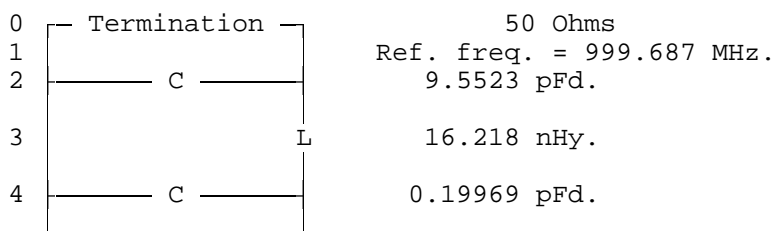
What ratio ? 1.25



[NORT:] Xform at branch 4

Preset ratio = .005

What ratio ? .8 (.8 is the inverse of 1.25)



5		C	1.6918 pFd.	
6	C		41.126 pFd.	
7.			Fx = 1037.9 MHz.	
10		C	2.4685 pFd.	
12	:-r-:		3.3207 pFd.	
11		L	37.389 Ohms	55.974 Deg.
			71.727 nHy.	
15	C		2.1488 pFd.	
16	L		2.9646 nHy.	
17.			Fx = 962.89 MHz.	
20		C	4.9748 pFd.	
22	:-r-:		84.761 nHy.	
21		L	12.5 Ohms	53.301 Deg.
			11.657 pFd.	
25	C		78.034 pFd.	
26		C	1.6649 pFd.	
27	C		0.19652 pFd.	
28		L	16.218 nHy.	
29	C		9.5523 pFd.	
30	Source		50 Ohms	
31	Fc = 999.69 MHz.			

As the last step, both resonators will be forced to the assumed 10 Ohms impedance needed for ceramic resonators.

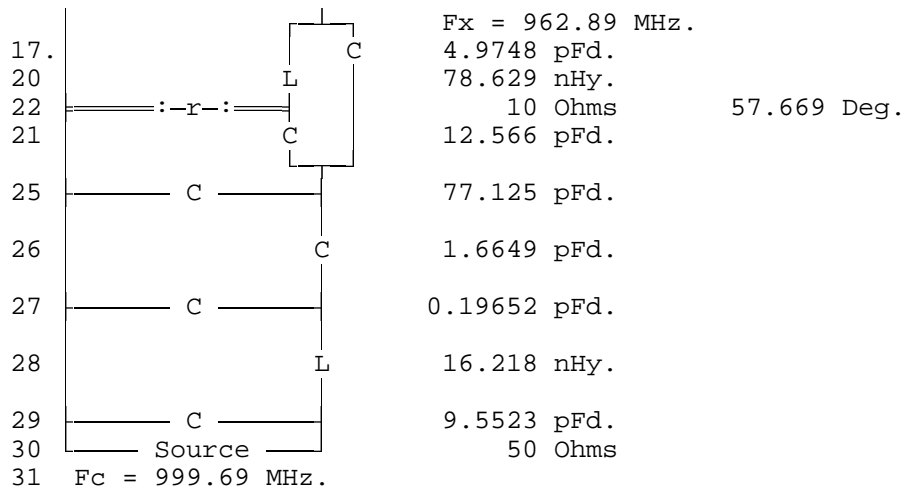
[MIS1:] Triplet 12

(Cr) to abort * What is new value (Ohms) ? 10

[MIS1:] Triplet 22

(Cr) to abort * What is new value (Ohms) ? 10

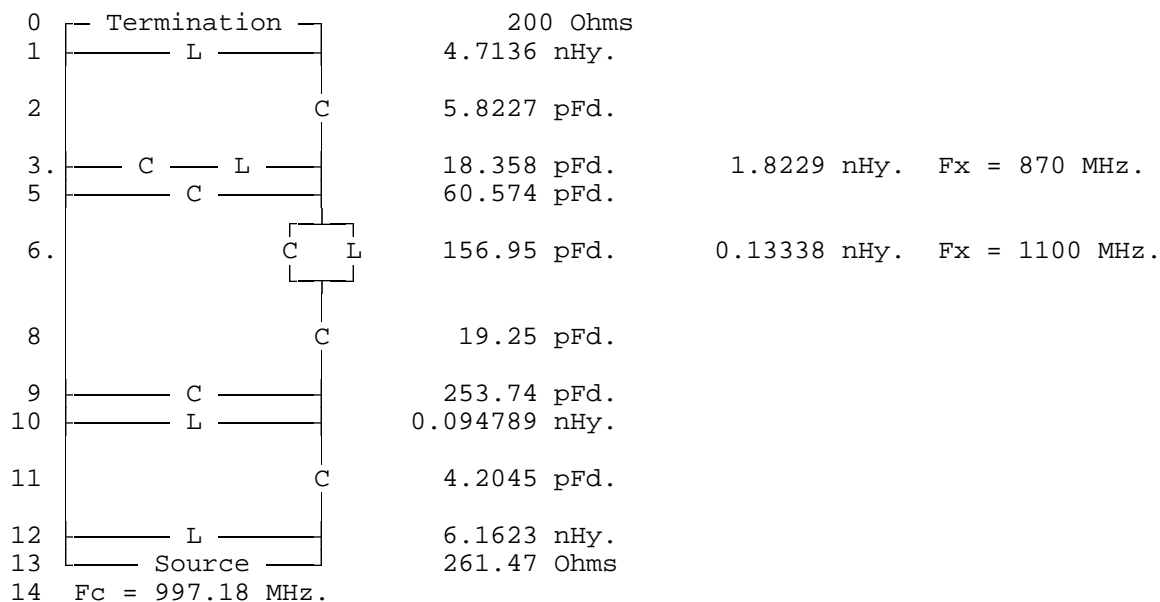
0	Termination		50 Ohms	
1			Ref. freq. = 999.687 MHz.	
2	C		9.5523 pFd.	
3		L	16.218 nHy.	
4	C		0.19969 pFd.	
5		C	1.6918 pFd.	
6	C		38.75 pFd.	
7.			Fx = 1037.9 MHz.	
10		C	2.4685 pFd.	
12	:-r-:		5.6965 pFd.	
11		L	9.9999 Ohms	73.16 Deg.
			41.811 nHy.	
15	C		2.1488 pFd.	
16	L		3.0636 nHy.	



*** Example 2 ***

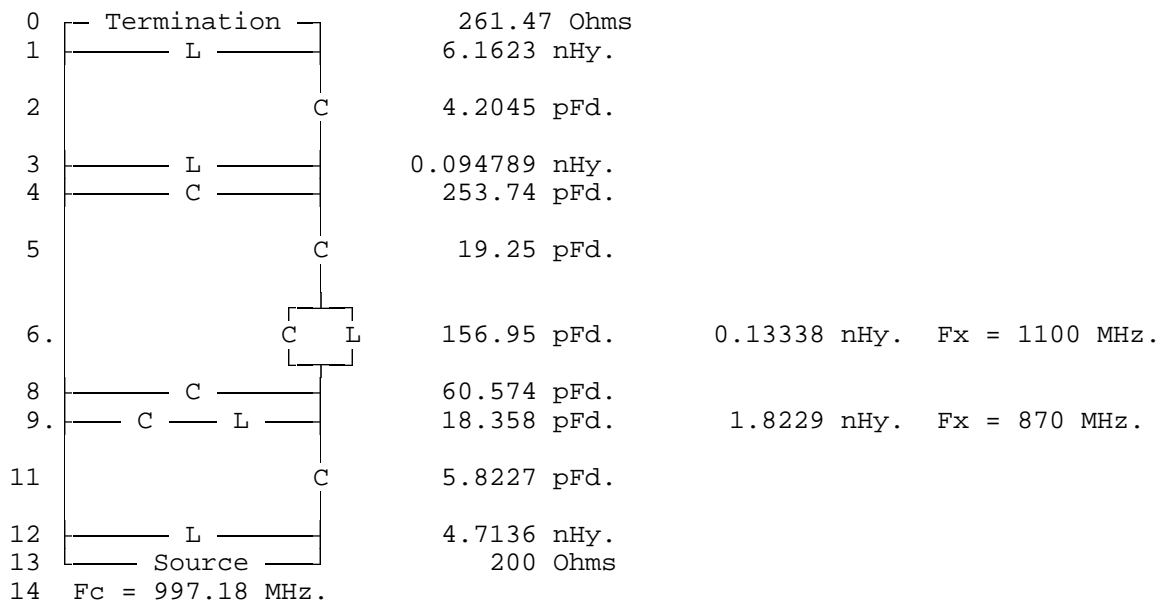
This example will illustrate how a fully pole placed filter can be converted for coupled triplets. It will also illustrate some of the things that might go wrong as you do the transformations.

Design = Conventional pole placer
 passband Ripple (0=Butt. dB) 0.05
 arithmetic Fo. MHz. 1000
 Bandwidth MHz. 150
 design Zo. 200
 tYpe: 1=sing 2=doub 3=ratio 2
 --- POLE PLACER DATA ---
 Zeros at zero (Dc.) = 5
 Zeros at Infinity = 1
 Finite transmission zero frequencies:
 870.000 1100.000
 Finite transmission zero sequence: 1 2
 Placer specification mask:



The first step is to reverse the filter end-for-end.

[main:] Reverse

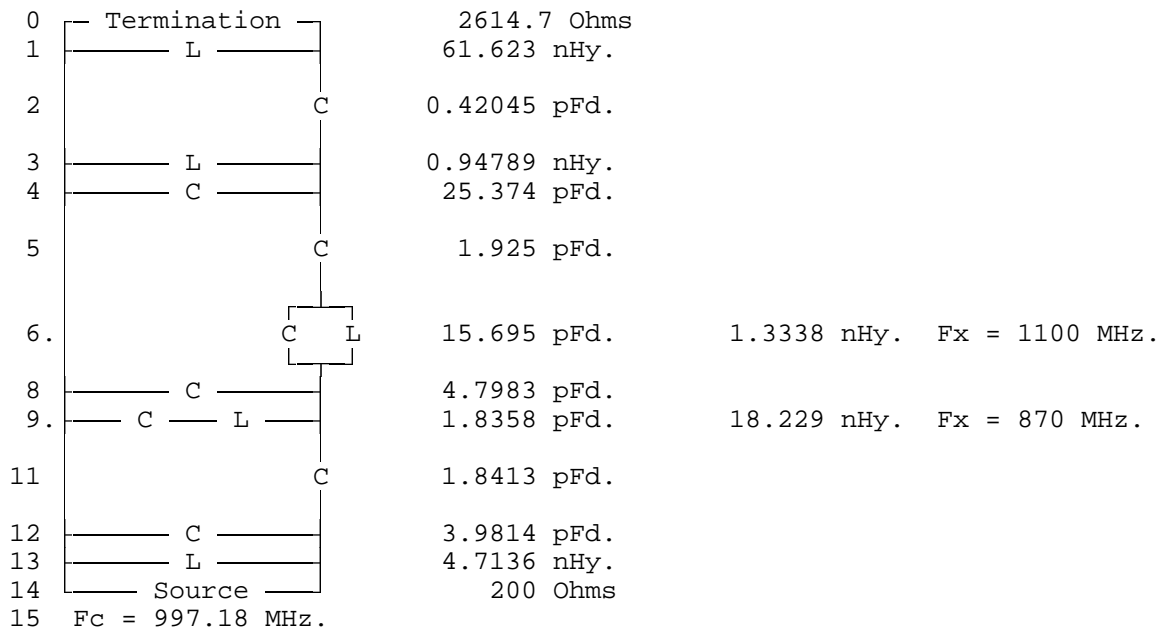


At this point, a capacitor is needed in parallel with the inductor at branch 12. It is also going to be necessary to raise the impedance of the network. A Norton transform at branch 11 will accomplish both requirements. The needed impedance ratio here is guess work since you don't know what part values will be generated by the second triplet that will provide the finite zero above the passband. Let's pick a value of 10.

[NORT:] Xform 11

Preset ratio = 1.00

What ratio ? 10



In order to form a network compatible with a coupled triplet at the shunt notch "trap" at branch 9, the series capacitor at branch 5 must be moved to the other side of the series notch "tank" at branch 6. This will also make the network at branches 2, 3 and 4 ready to accept a triplet for the high side finite zero.

[NORT:] Move branch 5

Position them after what branch number ? 6

0	Termination		2614.7 Ohms	
1	L		61.623 nHy.	
2		C	0.42045 pFd.	
3	L		0.94789 nHy.	
4	C		25.374 pFd.	
5.		C L	15.695 pFd.	1.3338 nHy. Fx = 1100 MHz.
7		C	1.925 pFd.	
8	C		4.7983 pFd.	
9.	C L		1.8358 pFd.	18.229 nHy. Fx = 870 MHz.
11		C	1.8413 pFd.	
12	C		3.9814 pFd.	
13	L		4.7136 nHy.	
14	Source		200 Ohms	
15	Fc = 997.18 MHz.			

Since the impedance ratio of 10 that was used to raise the impedance of the network earlier may not be correct, we will convert the section at branch 2 to a triplet to see what values are generated before generating the triplet at branch 8.

When the triplet command is used at a network having both a parallel L and C, as exist at branches 3 and 4, you have the option to select an impedance ratio that will scale the network from the triplet through to the termination. A ratio of .2 was chosen to bring the termination impedance down.

[MIS1:] Triplet at branch 3

Impedance ratio at triplet ? .2

0	Termination		522.87 Ohms	
1	L		12.323 nHy.	
2	C		1.7255 pFd.	
		C	Fx = 1100 MHz.	
3.		C	0.39059 pFd.	
6		C	-0.013622 pFd.	← NEGATIVE!
8	L		2639.9 nHy.	
9	C		1e-10 pFd.	
7		C	0.02233 pFd.	
11	L		2.2817 nHy.	← OK, for now.
12	C		9.4022 pFd.	
13		C	1.925 pFd.	
14	C		4.7983 pFd.	

15.	— C — L —	1.8358 pFd.	18.229 nHy.	Fx = 870 MHz.
17		1.8413 pFd.		
18	— C —	3.9814 pFd.		
19	— L —	4.7136 nHy.		
20	Source	200 Ohms		
21	Fc = 997.18 MHz.			

The results indicate that the ratio of 10 picked earlier for the Norton transform at the source end was ok since the values at branches 11 and 12 are reasonable. A different ratio will produce different values. The triplet equivalent itself has a negative value however. The reason for this is usually because the series capacitor at branch 2 (before the triplet command) was too small. This can be gotten around by splitting this capacitor into two caps in series, one capacitor can be larger than the other. The large one will be placed next to the triplet. To do this, back up using the OOps feature, split the series capacitor with one value set to 5 pFd, then interchange the two.

Oops (Mouse right button)

[NORT:] Split branch 2

(Press a mouse button or Cr for both equal)

Value of 1 part (pFd.) ? 5

[NORT:] Interchange branches 2,3

0	Termination	2614.7 Ohms		
1	— L —	61.623 nHy.		
2		0.45905 pFd.		
3		5 pFd.		
4	— L —	0.94789 nHy.		
5	— C —	25.374 pFd.		
6.	<div style="display: inline-block; vertical-align: middle;"> <div style="border: 1px solid black; padding: 2px; display: inline-block;">C</div> <div style="display: inline-block; vertical-align: middle; text-align: center;"> <div style="border: 1px solid black; width: 10px; height: 10px; margin: 0 auto;"></div> <div style="border: 1px solid black; padding: 2px; display: inline-block;">L</div> </div> </div>	15.695 pFd.	1.3338 nHy.	Fx = 1100 MHz.
8		1.925 pFd.		
9	— C —	4.7983 pFd.		
10.	— C — L —	1.8358 pFd.	18.229 nHy.	Fx = 870 MHz.
12		1.8413 pFd.		
13	— C —	3.9814 pFd.		
14	— L —	4.7136 nHy.		
15	Source	200 Ohms		
16	Fc = 997.18 MHz.			

Now we can try again to get the triplet.

[MIS1:] Triplet at branch 4

(Press a mouse button or Cr = 1.0) Impedance ratio at triplet ? .2

0	Termination	522.94 Ohms
1	— L —	12.325 nHy.
2		2.2953 pFd.

3	C	18.478 pFd.	
4.		Fx = 1100 MHz.	
7		3.809 pFd.	
9	L	2.7133 pFd.	
10	C	13.596 nHy.	
8		1e-10 pFd.	
	L	30.544 nHy.	
12	L	2.4061 nHy.	
13	C	6.5391 pFd.	
14		1.925 pFd.	
15	C	4.7983 pFd.	
16.	C L	1.8358 pFd.	18.229 nHy. Fx = 870 MHz.
18		1.8413 pFd.	
19	C	3.9814 pFd.	
20	L	4.7136 nHy.	
21	Source	200 Ohms	
22	Fc = 997.18 MHz.		

With the triplet inserted, we can proceed to generate a capacitor in parallel with the inductor at branch 1 by applying a Norton transform at branch 2. A ratio of .5 will return the termination to where it was and generate the needed capacitor.

[NORT:] Xform at branch 2

Preset ratio = 1.00

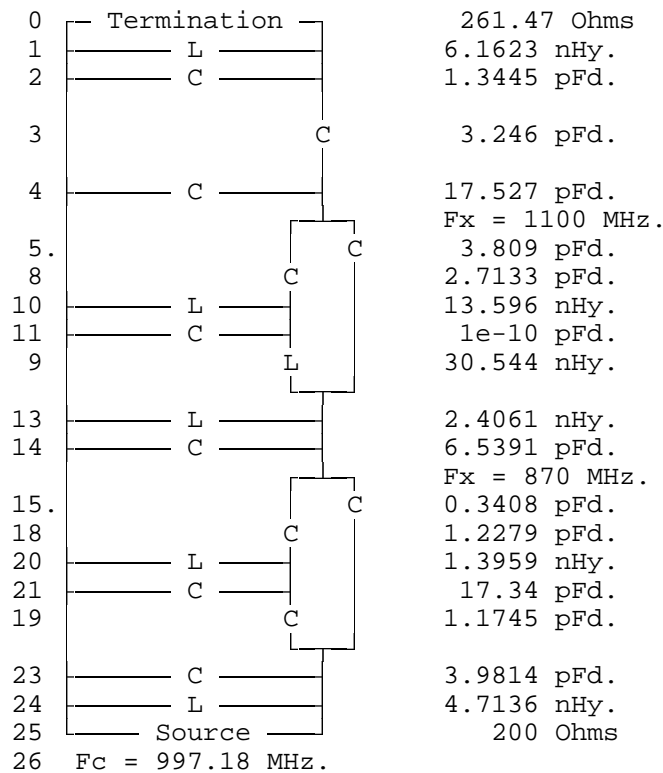
What ratio ? .5

0	Termination	261.47 Ohms	
1	L	6.1623 nHy.	
2	C	1.3445 pFd.	
3		3.246 pFd.	
4	C	17.527 pFd.	
5.		Fx = 1100 MHz.	
8		3.809 pFd.	
10	L	2.7133 pFd.	
11	C	13.596 nHy.	
9		1e-10 pFd.	
	L	30.544 nHy.	
13	L	2.4061 nHy.	
14	C	6.5391 pFd.	
15		1.925 pFd.	
16	C	4.7983 pFd.	
17.	C L	1.8358 pFd.	18.229 nHy. Fx = 870 MHz.
19		1.8413 pFd.	
20	C	3.9814 pFd.	
21	L	4.7136 nHy.	
22	Source	200 Ohms	

23 $F_c = 997.18 \text{ MHz.}$

Now, the finite zero generated by the "trap" at branch 16 can be converted to a triplet.

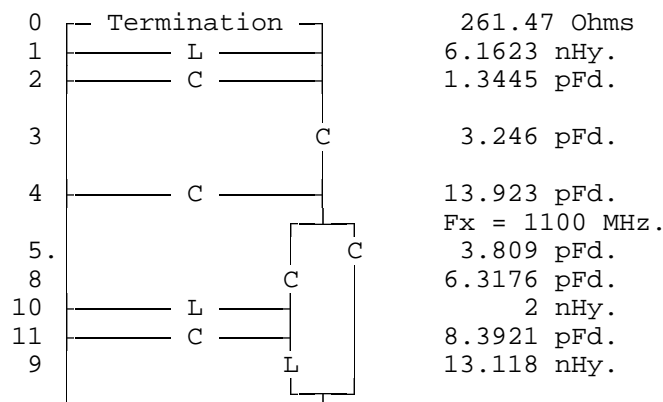
[MIS1:] Triplet at branch 16



Next, we would like to have values at the shunt "resonators" inside the triplets that are within a range that can be converted to shorted stub resonators. The values at branches 20 and 21 are ok as is. We will use the CT command again to make the values at the other triplet reasonable. Let's force 2 nHy. at branch 10.

[MIS1:] Triplet at branch 10

(Cr) to abort * What is new value (nHy.) ? 2



13	— L —	2.6873 nHy.
14	— C —	6.5391 pFd.
		Fx = 870 MHz.
15.		0.3408 pFd.
18	— C —	1.2279 pFd.
20	— L —	1.3959 nHy.
21	— C —	17.34 pFd.
19	— C —	1.1745 pFd.
23	— C —	3.9814 pFd.
24	— L —	4.7136 nHy.
25	Source	200 Ohms
26	Fc = 997.18 MHz.	

Now we can use the "LC to stub generator" to convert the L-C resonators inside both triplets to shorted stubs. Use the **Prog Stuber** command and choose the "V" option from the stub generator menu. Exit and use the **Stub** command to do the conversion.

[MIS:3] Program stuber (Pick option "V" on the menu)

[MIS3:] Stub at branch 10

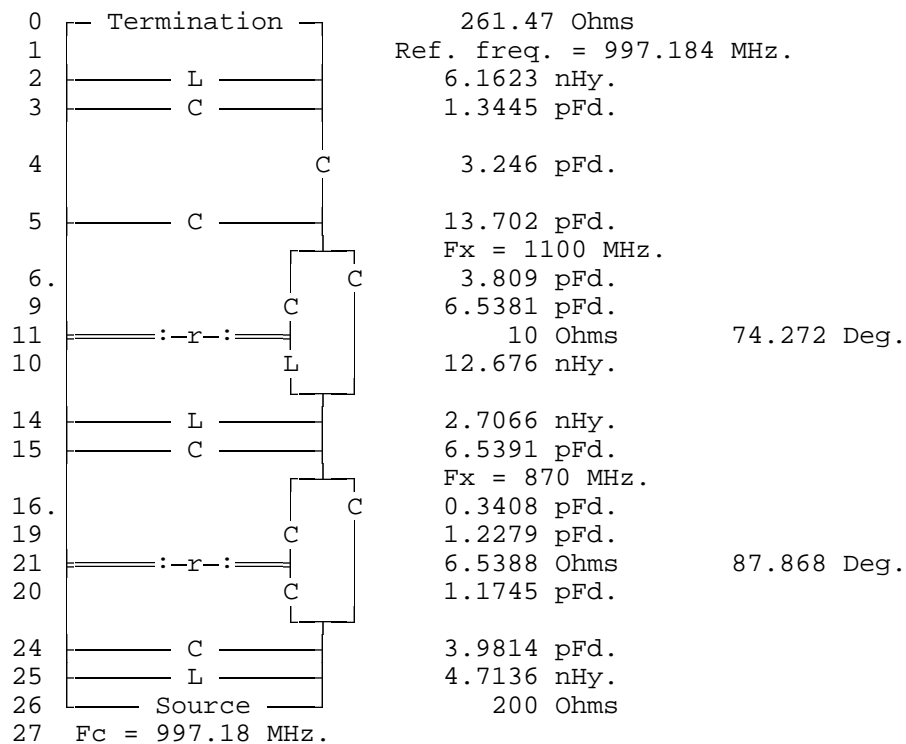
[MIS3:] Stub at branch 21 (This was branch 20 before the reference frequency branch was added by the stuber when branch 10 was converted)

0	Termination	261.47 Ohms	
1		Ref. freq. = 997.184 MHz. <-- added by stub generator.	
2	— L —	6.1623 nHy.	
3	— C —	1.3445 pFd.	
4	— C —	3.246 pFd.	
5	— C —	13.923 pFd.	
6.		Fx = 1100 MHz.	
9	— C —	3.809 pFd.	
11	==:-r:-==	6.3176 pFd.	
10	— L —	10.816 Ohms	73.595 Deg.
		13.118 nHy.	
14	— L —	2.6873 nHy.	
15	— C —	6.5391 pFd.	
		Fx = 870 MHz.	
16.		0.3408 pFd.	
19	— C —	1.2279 pFd.	
21	==:-r:-==	6.5388 Ohms	87.868 Deg.
20	— C —	1.1745 pFd.	
24	— C —	3.9814 pFd.	
25	— L —	4.7136 nHy.	
26	Source	200 Ohms	
27	Fc = 997.18 MHz.		

If quarter-wave ceramic dielectric resonators are to be used for the resonators, the correct impedance for these can be forced now by using the **Triplet** command again. This example assumes the resonators are 10 Ohms. The actual value will be specified by the manufacturer of the resonators. They are usually between 8 and 12 Ohms.

[MIS1:] Triplet at branch 11

(Cr) to abort * What is new value (Ohms) ? 10

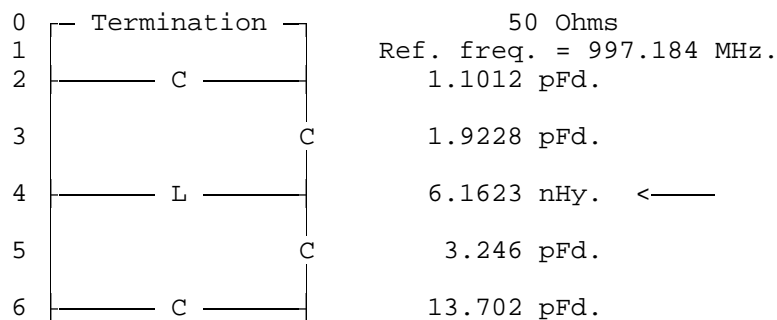


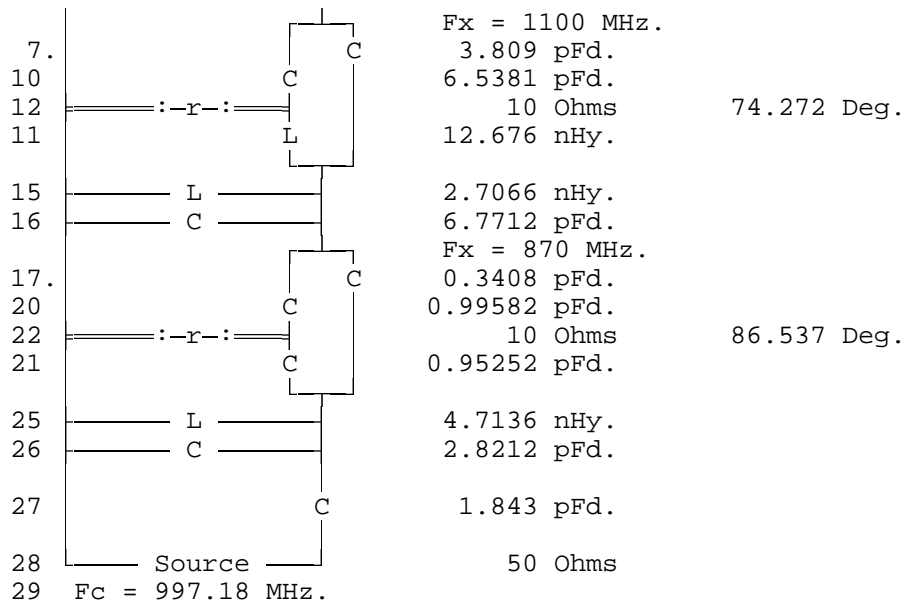
[MIS1:] Triplet at branch 21

(Cr) to abort * What is new value (Ohms) ? 10

The impedance matcher can be used now to match the load and source impedance to 50 Ohms. It is a good idea to save the network using the **Save** command before doing the impedance matching. This is the only way to back up after the filter has been source or load matched.

Two different matching networks were chosen at each end (option A and C). As it happened, the series C matching network if used on the source end (option A) would result in too small of a capacitor value across the termination end inductor. A capacitor of any value desired could be generated across the inductor at branch 4 by applying Norton transforms at branches 5 and 3 to lower the impedance at the inductor. The ratios would have to be N and 1.0 / N to maintain the 50 Ohm termination impedance.





A much better solution would be to recall the network saved before matching was applied and reduce the termination impedance to about 180 Ohms with a Norton transform at branch 3, then try the matching operation again. A series capacitor matching network would then yield acceptable values and fewer parts as well.

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